



## Sheet 1 Solution

### Problems:

**1.** The effect of the following opinions on Transmission Delay= & Propagation Delay:

| Option                                      | Transmission Delay | Propagation Delay |
|---|--------------------|-------------------|
| Increasing the packet size                  | Increasing         | Fixed             |
| Bit rate is doubled                         | be half            | Fixed             |
| Moving the two end points physically closer | Fixed              | Decreasing        |

**Note:** -Transmission Delay = Packet Size (P) / Bit Rate (R)

-Propagation Delay = Distance (D) / Propagation Speed(V)

**2.** Analog broadcast television channel has Bandwidth (B)= 6 MHZ

a) Using (256-QAM) signal & Symbol rate =  $6 \times 10^6$  QAM symbol/sec, So  
 Bit rate = Symbol rate \*  $\log_2 M$ , where M=number of bits per Symbol=256  
 Bit rate =  $6 \times 10^6 \times \log_2(256) = 48 \text{ Mbit/sec}$

b) In Noisy -Channel , according to Shannon Theorem :  
 Bit rate =  $B \times \log_2(1 + \text{SNR})$  where SNR=signal-to-noise-ratio, B=Bandwidth  
 So,  
 -  $48 \times 10^6 = 6 \times 10^6 \times \log_2(1 + \text{SNR})$   
 - **SNR= 255**

c) Band width is doubled (  $B_2 = 2 \times B_1$  )  
 -To have same the bit rate  
 -  $B_1 \times \log_2(1 + \text{SNR}_1) = B_2 \times \log_2(1 + \text{SNR}_2)$   
 -  $(\frac{1}{2}) \times \log_2(1 + \text{SNR}_1) = \log_2(1 + \text{SNR}_2)$   
 -  $\log_2(1 + \text{SNR}_1)^{\frac{1}{2}} = \log_2(1 + \text{SNR}_2)$   
 -  $(1 + \text{SNR}_2) = (1 + \text{SNR}_1)^{\frac{1}{2}}$   
 -  $\text{SNR}_1 = 255 \rightarrow \text{SNR}_2 = 15$   
 -  $\frac{\text{SNR}_2}{\text{SNR}_1} = \frac{\text{Signal}_2 \times \text{Noise}_1}{\text{Signal}_1 \times \text{Noise}_2} \& \frac{\text{Noise}_1}{\text{Noise}_2} = \frac{B_1}{B_2} = \frac{1}{2}$

$$\frac{Signal1}{Signal2} = \frac{30}{255}$$

**3.** Telephone Link is known to have Losses = 15 dB ,input power = 0.7 watt ,Output noise =5 uwatt .

- a) Output SNR(dB) = Output Power(dBw) - Output Noise(dBw),where:  
 - Output Power(dBw) = 10\*Log(Input Power) – Losses(dB)= -16.549 dBw  
 - Output Noise(dBw) = 10\*Log (Output Noise) = -42 dBw  
 So, **Output SNR(dB) = 25.451 dB**
- b) Capacity of this phone line = ? with a frequency range 300Hz-3300Hz:  
 Capacity = B\*Log<sub>2</sub> (1+SNR<sub>Out</sub>)  
 = **3000\*Log<sub>2</sub> (1+350.8) = 25.376 Kbit/sec**
- c) Phone line length = ? when phone line attenuation rate = 4 dB/Km , minimum output signal = 0.001watt & input signal = 0.7 watt :  
 Maximum attenuation inside line = 10\*Log<sub>10</sub>(Input Signal/Output Signal)  
 = 28.45 dB

$$\begin{aligned} \text{So, Phone line length} &\leq (\text{Maximum attenuation/attenuation rate}) \\ &\leq 28.45/4 \\ &\leq \mathbf{7.113 \text{ Km}} \end{aligned}$$

**4.** Ten 9600-bps lines

First : Capacity = ? for multiplexing these lines using Synchronous TDM

- Capacity = Number of lines \* bit rate of each line  
 = 10\*9600  
 = **96 Kbps**

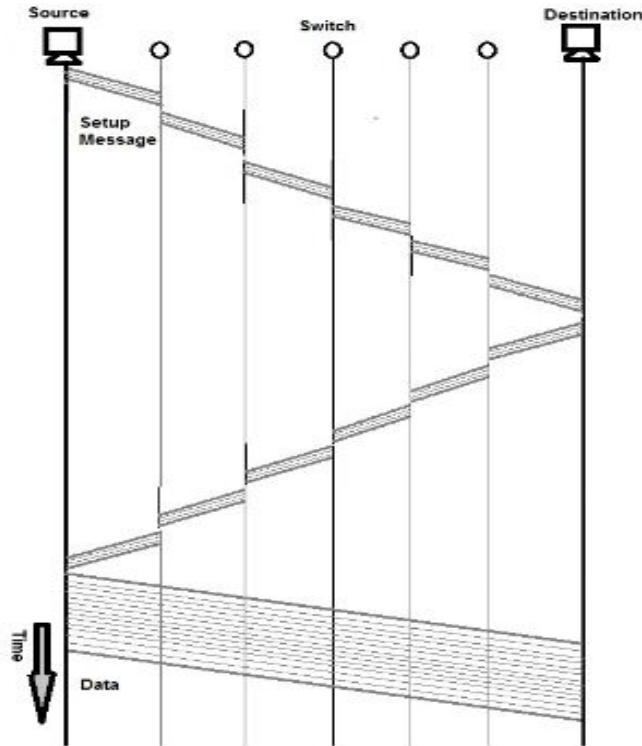
Second : Capacity = ? for statistical TDM assuming that link utilization = 0.8 & TDM link is busy 50 %

- Link utilization =  $\frac{\text{Actual\_Bit\_Rate}}{\text{Capacity}} = \frac{10*0.5*9600}{\text{Capacity}} = 0.8$   
 So, Capacity = **60 Kbps**

**5.** File is to be transmitted along a path composed of the source,destination and 5 switches .

- File Size = 5000-byte.
  - Link propagation Delay = 2 ms & bit rate = 4 Mbps.
  - Switch processing time (for packets & setup message) = 1 ms.
- Time needed to transfer the whole file = ? if:

a) Circuit Switching is used, Setup message= 1 KB (make one round trip)



Time Sequence Diagram

-Time needed to transfer this File ( T ) = Setup\_Time + Data \_Transfer\_Time ,

- Setup\_Time = 2 \* [ 6 \* P<sub>d</sub> + 6 \* Tr<sub>d(setup-message)</sub> + 5 \* Ts ],

- Data \_Transfer\_Time = 6 \* P<sub>d</sub> + Tr<sub>d(Data)</sub>

Where : - P<sub>d</sub> = Link propagation Delay = 2ms.

- Tr<sub>d</sub> = Transmission Delay

- Tr<sub>d(setup-message)</sub> =  $\frac{\text{Setup\_message\_Size}}{\text{Bit\_Rate}}$  = 2.048 ms.

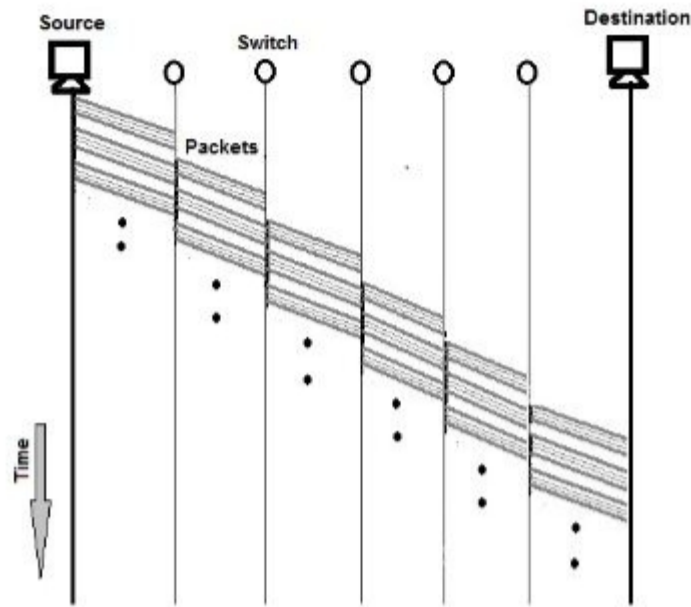
- Tr<sub>d(data)</sub> =  $\frac{\text{Data\_Size}}{\text{Bit\_Rate}}$  = 10 ms.

- Ts = Processing time = 1ms.

**So, Time needed to transfer this File ( T ) = 80.576 ms**

b) Packet Switching is used, Packet Size = 1KB = 1000 B (payload) + 24 B (header).

$$\text{So, Number of packets} = \frac{\text{File\_Size}}{\text{Payload}} = \frac{5000B}{1000B} = 5$$



Time Sequence Diagram

-Time needed to transfer this File ( T ) = Time to transfer first packet + Transmission Time of Remaining Packets in last link,

-Time to transfer first packet =  $6 * P_d + 6 * Tr_{d(packet)} + 5 * Ts$  ,

-Transmission Time of Remaining Packets in last link =  $(5-1) * Tr_{d(packet)}$

where : -  $P_d$  = Link propagation Delay = 2 ms.

-  $Tr_d$  = Transmission Delay

-  $Tr_{d(packet)} = \frac{Packet\_Size}{Bit\_Rate} = \frac{1 * 1024 * 8}{4 * 10^6} = 2.048 \text{ ms.}$

-  $Ts$  = Processing time = 1 ms.

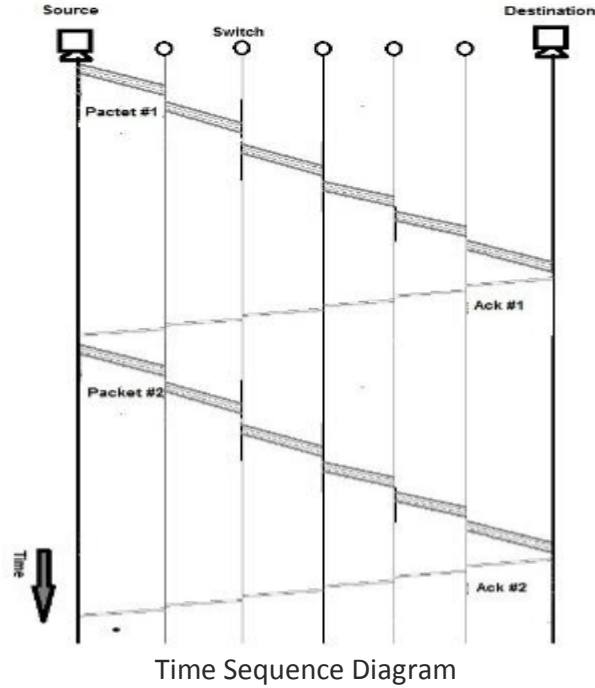
So, Time needed to transfer this File ( T ) = 37.48 ms.

&

**Link Utilization =**

$$\frac{Packet\_transmission\_time}{Packet\_transmission\_time + waiting\_time\_between\_two\_consecutive\_packets} = \frac{2.048ms}{2.048 + 0} = 100\%$$

c) Packet Switching with acknowledge is used, Packet Size = 1 byte.



- Time needed to transfer this File ( T ) = Number of packets \* [ Time to transfer packet + Time of receiving Packet Acknowledge]

- Time to transfer packet =  $6 * P_d + 6 * Tr_{d(packet)} + 5 * Ts$ ,
  - Time of receiving Packet Acknowledge =  $6 * P_d + 6 * Tr_{d(Ack)} + 5 * Ts_{(Ack)}$ ,
- where :
- $P_d$  = Link propagation Delay = 2 ms.
  - $Tr_d$  = Transmission Delay

$$- Tr_{d(packet)} = \frac{Packet\_Size}{Bit\_Rate} = \frac{1 * 1024 * 8}{4 * 10^6} = 2.048 \text{ ms.}$$

$$- Tr_{d(Ack)} = \frac{Ack\_Size}{Bit\_Rate} = \frac{1 * 8}{4 * 10^6} = 2 \text{ us. (negligible)}$$

- $Ts$  = Processing time = 1 ms.
- $Ts_{(Ack)}$  (negligible)

**So, Time needed to transfer this File ( T ) = 206.44 ms.**

& **Link Utilization =**

$$\frac{Packet\_transmission\_time}{Packet\_transmission\_time + waiting\_time\_between\_two\_consecutive\_packets}$$

$$= \frac{2.048ms}{29.288ms + 12ms} = 4.9 \%$$

**6.** Users share a 5 Mbps link, each user requires 500 Kbps where it is active &  $P(\text{active}) = 0.25$ .

a) With Circuit switching, Number of users can be supported =  $\frac{5Mbps}{500kbps} = 10$  users.

b) With Packet switching, 50 user

-Probability that 10 users are active =  ${}^{50}C_{10} * (.25)^{10} * (.75)^{40}$ .

c) With Packet switching, 50 user

-Probability that at least 10 users are active =  $\sum_{i=10}^{50} {}^{50}C_i * (.25)^i * (.75)^{50-i}$ .

d) Number of Users(N) = ?

$$1 - \sum_{i=10}^N {}^NC_i * (.25)^i * (.75)^{N-i} \geq .05 \rightarrow \text{get N.}$$

## 7.

In solving this problem, reference will be made to figures in Problem#5.

### **For Circuit Switching**

T = End-to-end delay

= Call Setup Time + Message Delivery Time

= Call Setup Time + Propagation Delay + Transmission Time

= S + NXD + L/B

= 0.537 sec

### **Datagram Packet Switching**

T = End-to-end delay

= Time to Transmit and Deliver all packets through first hop + Time to Deliver last packet across second hop + Time to Deliver last packet across third hop + Time to Deliver last packet across forth hop

= D1 + D2 + D3 + D4

There are P - H = 1024 - 16 = 1008 data bits per packet. A message of 3200 bits requires four packets (3200 bits/1008 bits/packet = 3.17 packets which we round up to 4 packets).

$$D1 = 4xt + p$$

where

t = transmission time for one packet

p = propagation delay for one hop

$$D1 = 4x(P/B) + D$$

$$= 0.428$$

$$D2 = D3 = D4 = t + p$$

$$= (P/B) + D$$

$$= 0.108$$

$$T = 0.752 \text{ sec}$$

### **Virtual Circuit Packet Switching**

$$\begin{aligned}T &= \text{End-to-end delay} \\&= \text{Call Setup Time} + \text{Datagram Packet Switching Time} \\&= S + \text{Datagram Packet Switching Time} \\&= 0.952 \text{ sec}\end{aligned}$$

### **b. Circuit Switching vs. Diagram Packet Switching**

$$\begin{aligned}T_c &= \text{End-to-End Delay, Circuit Switching} \\&= S + N \times D + L/B\end{aligned}$$

$$\begin{aligned}T_d &= \text{End-to-End Delay, Datagram Packet Switching} \\&= \text{Time to Transmit and Deliver all packets through first hop} + (N-1) \times \text{Time to Deliver last packet through a hop} \\&= N_p(P/B) + D + (N-1) \times (P/B + D)\end{aligned}$$

where

$$N_p = \text{Number of packets} = \left\lceil \frac{L}{P-H} \right\rceil$$

$$T_c = T_d$$

$$S + L/B = (N_p + N - 1)(P/B)$$

### **Circuit Switching vs. Virtual Circuit Packet Switching**

$$\begin{aligned}T_v &= \text{End-to-End Delay, Virtual Circuit Packet Switching} \\&= \text{Setup Time} + \text{End-to-End Delay, Datagram Packet Switching} \\&= S + T_d \\&= S + (N_p + N - 1)(P/B) + N \times D\end{aligned}$$

$$T_v = T_c$$

$$L/B = (N_p + N - 1)(P/B)$$