## Sheet 2

## BJT as an amplifier

## Problem (1):

Using the T equivalent model of the BJT, sketch the equivalent circuit of a transistor amplifier which a resistance $\left(\mathrm{R}_{\mathrm{E}}\right)$ is connected between the emitter \& the ground, the collector is grounded \& an input signal source $\left(\mathrm{v}_{\mathrm{b}}\right)$ is connected between the base \& the ground (It's assumed that the transistor is properly biased to operate in active mode). Show that:
a. The voltage gain between the base \& the emitter is given by:

$$
\frac{v_{e}}{v_{b}}=\frac{R_{E}}{R_{E}+r_{e}}
$$

b. The input resistance $\left(\mathrm{R}_{\mathrm{in}}\right)$ :

$$
R_{i n}=\frac{v_{b}}{i_{b}}=(\beta+1)\left(R_{E}+r_{e}\right)
$$

## Problem (2):

The transistor in the figure below is biased to operate in the active mode. Assuming that $\beta$ is very large, find the collector bias current $\left(\mathrm{I}_{\mathrm{C}}\right)$. Replace the transistor with the small-signal equivalent model (T-model with CCCS) and analyze the resulting amplifier equivalent circuit to show that:

$$
\frac{v_{o 1}}{v_{o 2}}=-\frac{R_{c}}{R_{e}}
$$



## Problem (3):

For the common emitter shown below: $\mathrm{V}_{\mathrm{CC}}=9 \mathrm{v}, \mathrm{R}_{1}=27 \mathrm{k} \Omega, \mathrm{R}_{2}=15 \mathrm{k} \Omega$, $\mathrm{R}_{\mathrm{E}}=1.2 \mathrm{k} \Omega$ and $\mathrm{R}_{\mathrm{C}}=2.2 \mathrm{k} \Omega$. The transistor $\beta=100$ and $\mathrm{V}_{\mathrm{A}}=100 \mathrm{v}$. Calculate the dc bias current $\mathrm{I}_{\mathrm{E}}$. If the amplifier is operating between a source resistance $\mathrm{R}_{\mathrm{s}}=10 \mathrm{k} \Omega$ and a load resistance $\mathrm{R}_{\mathrm{L}}=2 \mathrm{k} \Omega$, replace the transistor with its hybrid $\pi$-mode and find the value of $R_{i n}$, the voltage gain $\left(\mathrm{v}_{\mathrm{o}} / \mathrm{v}_{\text {sig }}\right)$ and the current gain $\left(\mathrm{i}_{\mathrm{o}} / i_{\mathrm{i}}\right)$.


## Problem (4):

In the circuit shown below, $\left(\mathrm{v}_{\text {sig }}\right)$ is a small signal sine wave with a zero average. The transistor $\beta$ is 100 .
a. Find the value of $R_{E}$ to establish a dc emitter current of about 1 mA .
b. Find the value of $R_{C}$ to establish a dc collector voltage of +5 v .
c. For $R_{L}=5 \mathrm{k} \Omega$ and the transistor $\mathrm{r}_{\mathrm{o}}=100 \mathrm{k} \Omega$, draw the small-signal equivalent circuit of the amplifier and determine its overall voltage gain, $\mathrm{R}_{\text {in }}$ and $\mathrm{R}_{\text {out }}$.


## Problem (5):

The amplifier below consists of two identical common-emitter amplifiers connected in cascade. Observe that the input resistance of the second stage, $\mathrm{R}_{\mathrm{in} 2}$, acts as the load resistance of the second stage.
a. For $\mathrm{V}_{\mathrm{CC}}=15 \mathrm{v}, \mathrm{R}_{1}=100 \mathrm{k} \Omega, \mathrm{R}_{2}=47 \mathrm{k} \Omega, \mathrm{R}_{\mathrm{E}}=3.9 \mathrm{k} \Omega, \mathrm{R}_{\mathrm{C}}=6.8 \mathrm{k} \Omega$ and $\beta=100$, determine the dc collector current and collector voltage of each transistor.
b. Draw the small-signal equivalent circuit of the entire amplifier and give the values of its entire component. Neglect $\mathrm{r}_{\mathrm{o} 1} \& \mathrm{r}_{\mathrm{o} 2}$.
c. Find $\mathrm{R}_{\mathrm{in} 1}$ and $\frac{v_{b 1}}{v_{\text {sig }}}$ for $\mathrm{R}_{\mathrm{s}}=5 \mathrm{k} \Omega$.
d. Find $\mathrm{R}_{\mathrm{in} 2}$ and $\frac{v_{b 2}}{v_{b 1}}$.
e. For $\mathrm{R}_{\mathrm{L}}=2 \mathrm{k} \Omega$, find $\frac{v_{0}}{v_{b 1}}$.
f. Find the overall voltage gain $\frac{v_{o}}{v_{s i g}}$.


## Problem (6):

Consider the common base amplifier in the figure below with a $10 \mathrm{k} \Omega$ load resistance connected to the collector via a large capacitance. Let $\mathrm{R}_{\mathrm{C}}=10 \mathrm{k} \Omega$, $V_{C C}=10 \mathrm{v}$ and $\mathrm{R}_{\mathrm{s}}=50 \Omega$.
a. To what value must (I) be set in order that the input resistance at Emitter is equal to that of the source (namely $50 \Omega$ )? What is the resulting voltage gain from the source to the load?
(Assume $\alpha=1$ ).
b. Find the voltage gain $\left(\mathrm{A}_{\mathrm{v}}\right)$ for $\mathrm{R}_{\mathrm{L}}=10 \mathrm{k} \Omega$.


## Problem (7):

For the circuit shown, called a boot-strapped follower:
a. Find the dc emitter current, $\mathrm{g}_{\mathrm{m}}, \mathrm{r}_{\mathrm{o}}$ and $\mathrm{r}_{\pi}$. Use $\beta=100$.
b. Replace the BJT with its hybrid $\pi$-model (neglecting $\mathrm{r}_{\mathrm{o}}$ ) and analyze the circuit to determine the input resistance $\left(\mathrm{R}_{\text {in }}\right)$ and the voltage gain $\left(\mathrm{v}_{\mathrm{o}} / \mathrm{v}_{\mathrm{sig}}\right)$.
c. Repeat (b) for the capacitor at the emitter is open circuit. Compare the results with those obtained in (b) to find the advantages of bootstrapping.


